

## Class 15, 5/18/15: The Phonetics of Rajaz Singing in Hausa

### 1. Readings and assignments

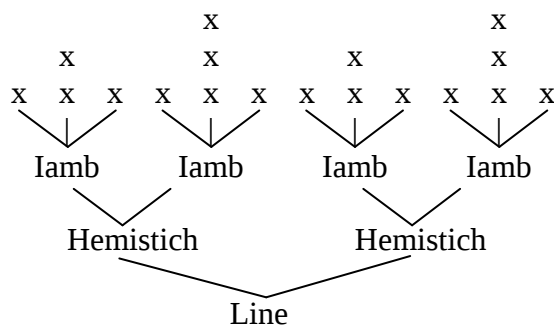
- Read in preparation for next week: Bruce Hayes and Claire Moore-Cantwell. [Gerard Manley Hopkins's sprung rhythm: corpus study and stochastic grammar](#). *Phonology* 28:235-282. On course web site.
- Class presentations now scheduled for 10th week.

### 2. Overall purpose of our rajaz project

- Study a sung metrical tradition all the way up and down (albeit with a thin slice)
  - meter
  - sung rhythm
  - phonetic realization of sung rhythm
- Today: cover the second two, building on our earlier work on pure meter (Classes 6 and 7).

### METRICS OF THE RAJAZ: REVIEW

### 3. Metrical pattern



*Levels of grid strength*  
superstrong  
strong  
weak

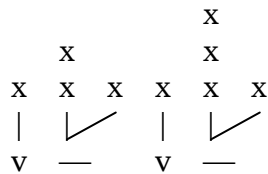
### 4. Five predominant types of realization for hemistichs

|                  |                    |      |                  |   |        |
|------------------|--------------------|------|------------------|---|--------|
| <b>v - v -</b>   | <b>iambic</b>      | 1362 | <b>- v - -</b>   | 6 | ignore |
| <b>- - -</b>     | <b>hemiola</b>     | 871  | <b>- v v v</b>   | 5 | ignore |
| <b>- v v -</b>   | <b>medial vv</b>   | 687  | <b>v v - v -</b> | 5 | ignore |
| <b>- - v -</b>   | <b>heptamoraic</b> | 600  | <b>- - - -</b>   | 2 | ignore |
| <b>v v - -</b>   | <b>initial vv</b>  | 417  | <b>v v - v</b>   | 2 | ignore |
| <b>v - v v</b>   | ignore             | 35   | <b>- v - v -</b> | 1 | ignore |
| <b>v v v -</b>   | ignore             | 24   | <b>- v v - -</b> | 1 | ignore |
| <b>v - -</b>     | ignore             | 19   | <b>- v v v v</b> | 1 | ignore |
| <b>v v v v -</b> | ignore             | 19   | <b>v v -</b>     | 1 | ignore |

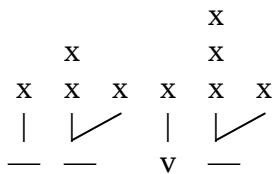
|         |        |    |           |   |        |
|---------|--------|----|-----------|---|--------|
| v - - - | ignore | 16 | v v v - - | 1 | ignore |
| - v -   | ignore | 10 | v v v v - | 1 | ignore |
| - - v v | ignore | 6  | v v v v v | 1 | ignore |

## 5. How the five types line up against the grid

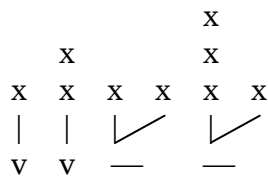
- Iambic (default foot type)



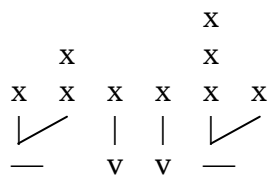
- Heptamoraic



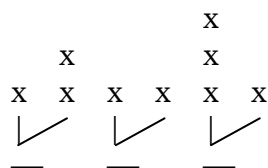
- Initial v v



- Medial v v



- Hemiola



## 6. There are various ways to sing the rajaz

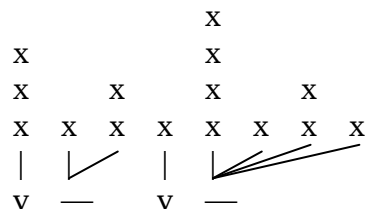
- You can sing it “straight”, in 6/8 time, so the grids of meter and song are the same.
- We will examine a rather different rendering:
  - Performance of “Tutocin Shehu” by Abubakar Ladan

## 7. Abubakar Ladan’s sung grid

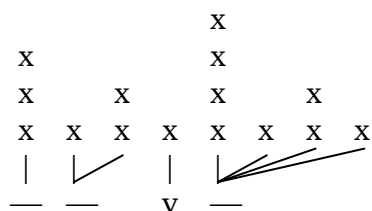
- This is rather straightforwardly related to the grid of the meter:
  - add two more positions per hemistich (6 → 8)
  - these get associated with the last heavy of each hemistich, which thus gets a total of four grid slots — perhaps SUPERSTRONG IS LONG
  - Following Lerdahl/Jackendovian principles, we’ll assume pervasive binarity for the sung grid — meaning that the syncopation is distributed differently than in the meter.

## 8. The Five Feet in AL’s sung grid

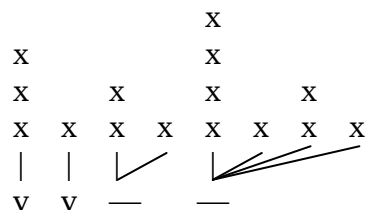
- Iambic



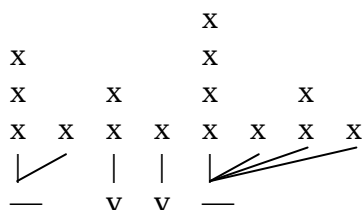
- Heptamoraic



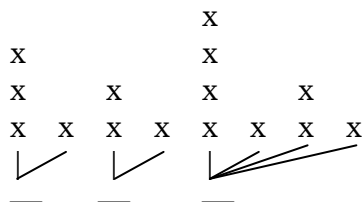
- Initial v v



- Medial v v



- Hemiola



## 9. Let us listen

- Caution: text is from a published source, and does not reflect the corrections Russ made upon listening.

|                            |                   |
|----------------------------|-------------------|
| Kanoo ta Abdu shaa yaboo   | v — v — / v — v — |
| Duk wanda kee bidxar raboo | — — v — / v — v — |
| Akwai shi can zuboo-zuboo  | v — v — / v — v — |
| Ka tabbataa fa Maddibo     | v — v — / v — v — |
| Doomin fadxaa ta gaskiya   | — — v — / v — v — |

|                          |                   |
|--------------------------|-------------------|
| Sai zuuciyar Niijeeriyaa | — — v — / v — v — |
| Sakkwato birnin manyaa   | — v v — / — — —   |
| Koo daa a yau koo a jiya | — — v — / — v v — |
| Suu muka bi da gaskyaa   | — v v — / v — v — |
| Garin da baabu tooshiyaa | v — v — / v — v — |

|                           |                   |
|---------------------------|-------------------|
| Barno bulaakaa birnii     | — — v — / — — —   |
| Ta Sheehu gun Kxuuraani   | v — v — / — — —   |
| Tsohon garin addiinii     | v — v — / — — —   |
| Koo zaamanii yai zaamanii | v — v — / v — v — |
| Ba zaa su kauce gaskiyaa  | v — v — / v — v — |

|                          |                   |
|--------------------------|-------------------|
| Gwandu ta Maalam Haruuna | — v v — / — v — — |
| Garin da baa maasu zinaa | v — v — / — v v — |
| Baa maasu almudanhanaa   | v — v — / — v v — |
| Dukan tafarkin bxarnaa   | v — v — / — — —   |
| Yaa hana yii gabaa dxaya | — v v — / v — v — |

|                         |                   |
|-------------------------|-------------------|
| Babban garii Hadxeejiya | v — v — / v — v — |
|-------------------------|-------------------|

|                           |                   |
|---------------------------|-------------------|
| Garin da baa a shan giyaa | v — v — / v — v — |
| Baa sansanin magaajiyaa   | v — v — / v — v — |
| Baa kxaryaa da faariyaa   | — — — / v — v —   |
| Sai hanyaa ta gaskiyaa    | — — — / v — v —   |
| Mun zoo ga Birnin Katsina | v — v — / — v v — |
| Garin mazaa Usmaana       | v — v — / — — —   |
| Garin Walii Dxam marinaa  | v — v — / — v v — |
| Yai shaharaa a koo inaa   | — v v — / v — v — |
| Kan ilmi da gaskiyaa      | — — — / v — v —   |
| Mu gangaraa Adamaawaa     | v — v — / v v — — |
| Garin dxiya baa baawaa    | v — v — / — — —   |
| Wurin gyadxaa gun daawaa  | v — v — / — — —   |
| Abinci naa nan da yawaa   | v — v — / — v v — |
| Da arziki na saaniyaa     | v — v — / v — v — |
| Da arziki da abinci       | v — v — / v — v — |
| Da gaskiyaa da mutuncii   | v — v — / v v — — |
| Da tattalii da zumuncii   | v — v — / v v — — |
| An san mutaanen Bauci     | v — v — / — — —   |
| Bin sharixaa ta gaskiya   | — v v — / v — v — |
| Zaariya babban birnii     | — v v — / — — —   |
| Garii da maasu sukuunii   | v — v — / v v — — |
| Da maasu aikii da sanii   | v — v — / — v v — |
| Nan aka cee wa sansani    | — v v — / v — v — |
| Areewa baabu saakiyaa     | v — v — / v — v — |
| Gumel garin Muhammadu     | v — v — / v — v — |
| Na-sooro dxam Muhammadu   | v — v — / v — v — |
| Garin da baabu faasiduu   | v — v — / v — v — |
| Baa nakxasi da ziyaaduu   | — v v — / v v — — |
| Kan kxaulii na gaskiyaa   | — — — / v — v —   |

## THEORY AND ANALYSIS

### 10. A really simple theory (qualitative)

- Primary premise: what we see in phonetics is always a quantitative compromise between conflicting ends.
  - Flemming's treatment of the "locus effect" (readings) is a classic case.
- Second premise: not hard to implement this with maxent grammars; which give you a freebie learning angle
  - Flemming's is a harmonic grammar, though non-stochastic and not learned.

## 11. Laying out the basis for constraints (qualitative)

- Moras like to be isochronous.
- Syllables like to be isochronous.

→ Consequence so far: a heavy syllable is not really twice as long a light (true in Hausa and many other languages).

➤ I.e. light syllables are chubby moras.

- Grid columns like to be isochronous.

→ So crowding a heavy into one grid column, as in (8)-heptamoraic, will squeeze the heavy.

- Hemistichs like to be isochronous

→ several implications, below

## 12. What happens when the hemistichs try to be isochronous

- — — — : — can be quite long, since they need not share with chubby moras.
- Heptamoraic feet: non-initial syllables have to get shorter to compensate.

## 13. The foot taxonomy

- Heptamoraic

— — v —

- All are squeezed by the extra mora.
- All are lightly squeezed by the presence of the single chubby mora v.
- Initial — is especially squeezed by having just one grid slot.

- Iambic, Initial vv, Medial vv

v — v —, v v — —, — v v —

- All are somewhat squeezed by the presence of two fat moras v v.

- Hemiola

— — —

- Sitting pretty, no compression effects

## EMPIRICAL STUDY OF DURATION IN ABUBAKAR LADAN'S TUTOCIN SHEHU

**14. We<sup>1</sup> measured the syllables in stanzas**

- First twenty stanzas
- Actually syllable boundaries
  - Eventually, I think we'll need to use Donca Steriade's *intervals* instead (Ryan)
- We did the usual procedure nowadays: play recording in Praat, set textgrids, measure the durations with a downloadable script.

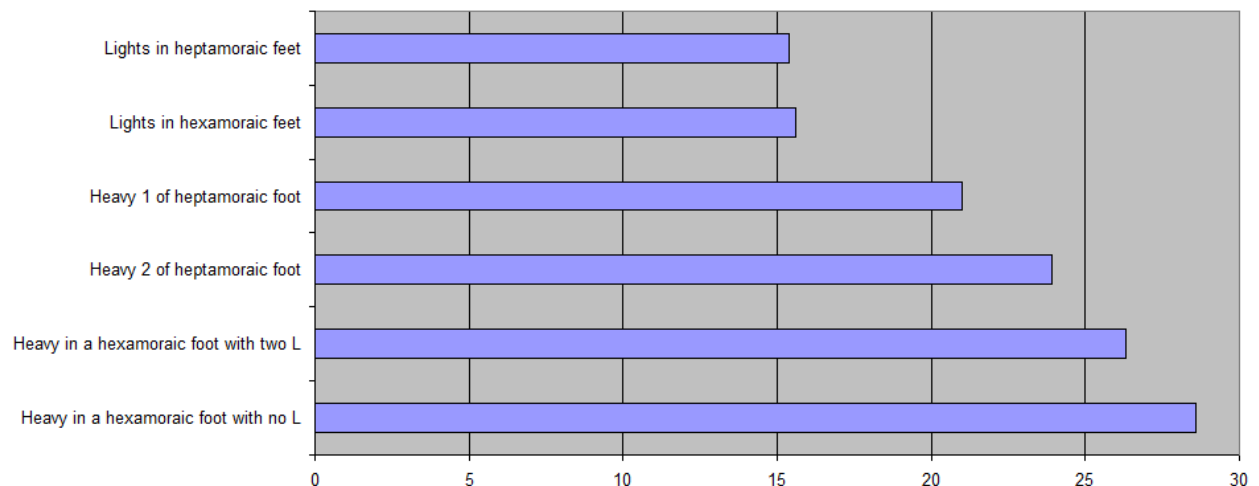
**15. Skipped data**

- Last syllable in each hemistich — these varied hugely, and often faded out into a pause; unmeasurable really.

**16. Averages**

- We need to find a sensible taxonomy

|   |                                       |      |
|---|---------------------------------------|------|
| ↕ | <i>Shortest</i>                       |      |
|   | Lights in heptamoraic feet            | 15.4 |
|   | Lights in hexamoraic feet             | 15.6 |
|   | Heavy 1 of heptamoraic foot           | 21.0 |
|   | Heavy 2 of heptamoraic foot           | 23.9 |
|   | Heavy in a hexamoraic foot with two L | 26.3 |
|   | Heavy in a hexamoraic foot with no L  | 28.6 |
| ↕ | <i>Longest</i>                        |      |



<sup>1</sup> Well, gee ... it was Russ, really. I tended to hear allophones instead of phonemes and was naïve in various other ways.

## 17. Significance testing

- We can do significance testing by making factors be *cutoff points* in this hierarchy, and doing a linear model (lm() in R).

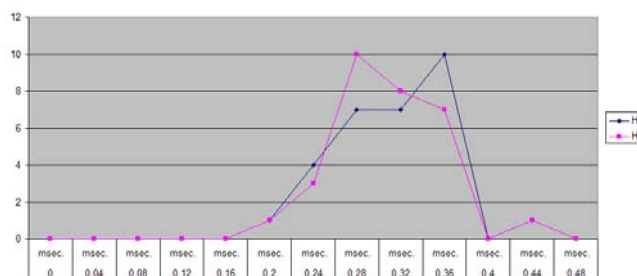
|                          | Estimate | Std. Error | t value | Pr(> t ) |     |
|--------------------------|----------|------------|---------|----------|-----|
| (Intercept)              | 0.153855 | 0.007707   | 19.963  | < 2e-16  | *** |
| At Least L Of Hexa       | 0.001747 | 0.008009   | 0.218   | 0.82742  |     |
| At Least Heavy           | 0.054124 | 0.008009   | 6.758   | 3.51e-11 | *** |
| At Least Heavy2 Of Hepta | 0.029517 | 0.010900   | 2.708   | 0.00697  | **  |
| At Least Heavy Of Hexa   | 0.023966 | 0.008288   | 2.892   | 0.00398  | **  |
| At Least Heavy Of HHH    | 0.023512 | 0.005535   | 4.247   | 2.53e-05 | *** |

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

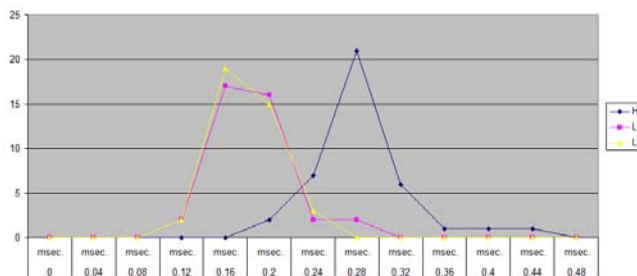
- Every distinction is coming out significant except the tiniest one ; i.e. lights in hepta vs. hexamoraic feet.
- I followed up and did the more professional version (a linear mixed-effects model, using lmer()), and got pretty much the same result.

## 18. Histograms (sort of) of the duration distributions

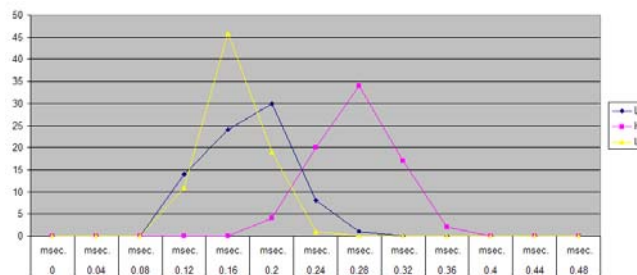
HHH:



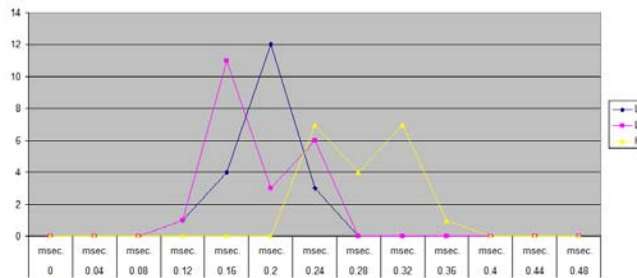
HLLH:



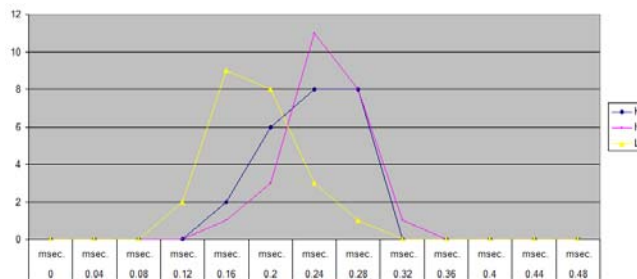
LHLH:



LLHH:



HHLH:



## THEORY

### 19. What we did

- Blend of
  - Flemming-style Harmonic Grammar generative phonetics (readings)
  - ... generalized with Maxent to get an actual spread of predicted values
  - ... implemented with maxent training regimen to match data
  - ... facilitated computationally by measuring time in 10 msec. intervals rather than as a continuum (countable number of candidates)
- This is rather similar to what Michael Lefkowitz is pursuing for his dissertation

### 20. Generative phonetics

- See e.g. early work of Keating:
  - P. A. Keating: "Universal phonetics and the organization of grammars", *Phonetic Linguistics*, ed. V. Fromkin, Academic Press, 115-132 (1985)
  - P. A. Keating: "The window model of coarticulation: articulatory evidence", in *Papers in Laboratory Phonology I*, ed. J. Kingston & M. Beckman, Cambridge University Press, pp. 451-470 (1990)

- Parameters of sound categories have *targets* (idealized perfect values).
- A grammar creates quantitative representations, guided by the abstract targets.
- Let's suppose as a wild approximation that the target is simply the *mean* across all tokens.
  - We can probably do better: median, or smoothed mode

## 21. Doing this with constraint-based grammars

- GEN consists of all possible phonetic representations
- The weights and math of Harmonic Grammar interface naturally with the quantitative representations.
- They let us pick the best phonetic representation, or (in maxent) a probability distribution across phonetic representations.

## 22. GEN

- We'll ignore the greatly lengthened final syllable of each hemistich — vast variation; too hard to measure — and just do the first “demihemistich”.
  - e.g. v — v of the iambic hemistich, etc.
- Find a suitable range for the duration of the two or three syllables of this demihemistich.
- Categorize at intervals of 10 msec., creating a fine grid of candidates.
  - This is pushing the limits of convenient file size and Maxent Grammar Tool run-time.

## 23. Part of the program interface (values in msec.)

The screenshot shows a window titled "Gen" with a list of parameters and their corresponding values in milliseconds. The parameters are organized into two groups: "Light" and "Heavy", each with "low limit", "high limit", and "increment" values.

| Parameter         | Value (msec.) |
|-------------------|---------------|
| Light, low limit  | 80            |
| Light, high limit | 280           |
| Light, increment  | 10            |
| Heavy, low limit  | 80            |
| Heavy, high limit | 350           |
| Heavy, increment  | 10            |

## 24. Eight Constraints for Hausa Recitation

again, values are measured in milliseconds

- SQUEEZE MORA
  - Assess a penalty of the square of the degree to which candidate mora duration exceeds the mean.

- STRETCH MORA
  - Assess a penalty of the square of the degree to which candidate mora duration falls short of the mean.
- SQUEEZE SYLLABLE
  - Assess a penalty of the square of the degree to which candidate syllable duration exceeds the mean.
- STRETCH SYLLABLE
  - Assess a penalty of the square of the degree to which candidate syllable duration falls short of the mean.
- SQUEEZE GRID COLUMN
  - Assess a penalty of the square of the degree to which candidate grid column duration exceeds the mean.
- STRETCH GRID COLUMN
  - Assess a penalty of the square of the degree to which candidate grid column duration falls short of the mean.
- SQUEEZE DEMIHEMISTICH
  - Assess a penalty of the square of the degree to which candidate demihemistich duration exceeds the mean.
- STRETCH DEMIHEMISTICH
  - Assess a penalty of the square of the degree to which candidate demihemistich duration falls short of the mean.

## 25. A few of the training data (Schuh measurements by demihemistich)

|         |           |           |           |
|---------|-----------|-----------|-----------|
| v - v - | 0.108001  | 0.2832495 | 0.1379933 |
| v - v - | 0.201906  | 0.270291  | 0.1939169 |
| - - v - | 0.1818279 | 0.2785149 | 0.137179  |
| v - v - | 0.1903456 | 0.3092762 | 0.1321906 |
| v - v - | 0.0889996 | 0.2963731 | 0.1869171 |
| v - v - | 0.1797749 | 0.2519127 | 0.191127  |
| v - v - | 0.0950104 | 0.2935951 | 0.1408302 |
| v - v - | 0.1550768 | 0.3015516 | 0.1607214 |
| - - v - | 0.2171749 | 0.2410821 | 0.159706  |
| v - v - | 0.1847428 | 0.2347169 | 0.1177563 |
| - - v - | 0.2458428 | 0.2373107 | 0.2167177 |
| - - v - | 0.2621213 | 0.2833985 | 0.1522181 |

## 26. The targets (crude means)

|                                   | <i>Mora</i> | <i>Syllable</i> | <i>Position</i> | <i>Demihemistich</i> |
|-----------------------------------|-------------|-----------------|-----------------|----------------------|
| <i>Mean</i>                       | 153         | 203             | 144             | 577                  |
| <i>Median</i>                     | 136         | 190             | 139             | 572                  |
| <i>Smoothed mode</i> <sup>2</sup> | 128         | 154             | 131             | 572                  |

## 27. A bit of the OT-Format candidate file<sup>3</sup>

- This demihemistich is — —, i.e. from a hemiola hemistich — — —.

<sup>2</sup> Replace each value with the average of itself and 20 tokens above and below it in the sorted distribution.

<sup>3</sup> Reformatted for clarity on this handout.

|             |              |        | SQUEEZE<br>MORA | STRETCH<br>MORA | SQUEEZE<br>SYLLABLE | STRETCH<br>SYLLABLE | SQUEEZE<br>POSITION | STRETCH<br>POSITION | SQUEEZE<br>METER | STRETCH<br>METER |
|-------------|--------------|--------|-----------------|-----------------|---------------------|---------------------|---------------------|---------------------|------------------|------------------|
|             |              | Winner |                 |                 |                     |                     |                     |                     |                  |                  |
| HHH+296+346 | HH0H+80+80   |        | 0.00            | 4.02            | 0.00                | 3.05                | 0.00                | 4.36                | 0.00             | 17.43            |
|             | HH0H+80+90   |        | 0.00            | 3.83            | 0.00                | 2.81                | 0.00                | 4.15                | 0.00             | 16.60            |
|             | HH0H+80+100  |        | 0.00            | 3.64            | 0.00                | 2.59                | 0.00                | 3.96                | 0.00             | 15.80            |
|             | HH0H+80+110  |        | 0.00            | 3.47            | 0.00                | 2.40                | 0.00                | 3.78                | 0.00             | 15.01            |
|             | HH0H+80+120  |        | 0.00            | 3.30            | 0.00                | 2.22                | 0.00                | 3.60                | 0.00             | 14.25            |
|             | HH0H+80+130  |        | 0.00            | 3.15            | 0.00                | 2.06                | 0.00                | 3.44                | 0.00             | 13.50            |
|             | HH0H+80+140  |        | 0.00            | 3.00            | 0.00                | 1.93                | 0.00                | 3.28                | 0.00             | 12.78            |
|             | HH0H+80+150  |        | 0.00            | 2.86            | 0.00                | 1.81                | 0.00                | 3.14                | 0.00             | 12.07            |
|             | HH0H+80+160  |        | 0.00            | 2.74            | 0.00                | 1.71                | 0.00                | 3.01                | 0.00             | 11.39            |
|             | HH0H+80+170  |        | 0.00            | 2.62            | 0.00                | 1.64                | 0.00                | 2.88                | 0.00             | 10.72            |
|             | HH0H+80+180  |        | 0.00            | 2.52            | 0.00                | 1.58                | 0.00                | 2.77                | 0.00             | 10.08            |
|             | HH0H+80+190  |        | 0.00            | 2.42            | 0.00                | 1.54                | 0.00                | 2.67                | 0.00             | 9.45             |
|             | HH0H+80+200  |        | 0.00            | 2.34            | 0.00                | 1.53                | 0.00                | 2.57                | 0.00             | 8.85             |
|             | HH0H+80+210  |        | 0.00            | 2.26            | 0.00                | 1.52                | 0.00                | 2.49                | 0.00             | 8.26             |
|             | HH0H+80+220  |        | 0.00            | 2.20            | 0.03                | 1.52                | 0.00                | 2.41                | 0.00             | 7.70             |
|             | HH0H+80+230  |        | 0.00            | 2.14            | 0.07                | 1.52                | 0.00                | 2.35                | 0.00             | 7.15             |
|             | HH0H+80+240  |        | 0.00            | 2.09            | 0.13                | 1.52                | 0.00                | 2.30                | 0.00             | 6.63             |
|             | HH0H+80+250  |        | 0.00            | 2.06            | 0.22                | 1.52                | 0.00                | 2.25                | 0.00             | 6.12             |
|             | HH0H+80+260  |        | 0.00            | 2.03            | 0.32                | 1.52                | 0.00                | 2.22                | 0.00             | 5.64             |
|             | HH0H+80+270  |        | 0.00            | 2.02            | 0.44                | 1.52                | 0.00                | 2.20                | 0.00             | 5.17             |
|             | HH0H+80+280  |        | 0.00            | 2.01            | 0.59                | 1.52                | 0.00                | 2.18                | 0.00             | 4.73             |
|             | HH0H+80+290  |        | 0.00            | 2.01            | 0.75                | 1.52                | 0.00                | 2.18                | 0.00             | 4.30             |
|             | HH0H+80+300  |        | 0.02            | 2.01            | 0.93                | 1.52                | 0.01                | 2.18                | 0.00             | 3.90             |
|             | HH0H+80+310  |        | 0.04            | 2.01            | 1.14                | 1.52                | 0.02                | 2.18                | 0.00             | 3.51             |
|             | HH0H+80+320  |        | 0.08            | 2.01            | 1.36                | 1.52                | 0.05                | 2.18                | 0.00             | 3.15             |
|             | HH0H+80+330  |        | 0.12            | 2.01            | 1.60                | 1.52                | 0.09                | 2.18                | 0.00             | 2.80             |
|             | HH0H+80+340  |        | 0.18            | 2.01            | 1.86                | 1.52                | 0.13                | 2.18                | 0.00             | 2.48             |
|             | HH0H+80+350  |        | 0.24            | 2.01            | 2.15                | 1.52                | 0.19                | 2.18                | 0.00             | 2.17             |
|             | HH0H+90+80   |        | 0.00            | 3.83            | 0.00                | 2.81                | 0.00                | 4.15                | 0.00             | 16.60            |
|             | HH0H+90+90   |        | 0.00            | 3.63            | 0.00                | 2.57                | 0.00                | 3.95                | 0.00             | 15.80            |
|             | HH0H+90+100  |        | 0.00            | 3.45            | 0.00                | 2.36                | 0.00                | 3.76                | 0.00             | 15.01            |
|             | HH0H+90+110  |        | 0.00            | 3.27            | 0.00                | 2.16                | 0.00                | 3.57                | 0.00             | 14.25            |
|             | HH0H+90+120  |        | 0.00            | 3.11            | 0.00                | 1.98                | 0.00                | 3.40                | 0.00             | 13.50            |
|             | HH0H+300+320 |        | 0.10            | 0.00            | 2.29                | 0.00                | 0.06                | 0.00                | 0.18             | 0.00             |
|             | HH0H+300+330 |        | 0.14            | 0.00            | 2.53                | 0.00                | 0.09                | 0.00                | 0.28             | 0.00             |
|             | HH0H+300+340 |        | 0.20            | 0.00            | 2.80                | 0.00                | 0.14                | 0.00                | 0.39             | 0.00             |
|             | HH0H+300+350 | 1      | 0.26            | 0.00            | 3.08                | 0.00                | 0.19                | 0.00                | 0.53             | 0.00             |
|             | HH0H+310+80  |        | 0.04            | 2.01            | 1.14                | 1.52                | 0.02                | 2.18                | 0.00             | 3.51             |
|             | HH0H+310+90  |        | 0.04            | 1.82            | 1.14                | 1.29                | 0.02                | 1.97                | 0.00             | 3.15             |

## 28. Weights obtained

|                       |      |
|-----------------------|------|
| SQUEEZE MORA          | 3.43 |
| STRETCH MORA          | 1.93 |
| SQUEEZE SYLLABLE      | 0.90 |
| STRETCH SYLLABLE      | 0.66 |
| SQUEEZE POSITION      | 1.12 |
| STRETCH POSITION      | 1.66 |
| SQUEEZE DEMIHEMISTICH | 0.48 |
| STRETCH DEMIHEMISTICH | 0.48 |

## 29. Best candidates for each foot type, with probability

| <i>Foot type</i> | <i>Quantities</i> | <i>Syl1</i> | <i>Syl2</i> | <i>Syl3</i> | <i>Probability of this candidate</i> |
|------------------|-------------------|-------------|-------------|-------------|--------------------------------------|
| Hemiola          | — — —             | 270         | 270         |             | 0.01032                              |
| Heptamoraic      | — — v —           | 210         | 260         | 150         | 0.001308                             |
| Medial v v       | — v v —           | 270         | 160         | 160         | 0.001649                             |
| Iambic           | v — v —           | 160         | 270         | 160         | 0.001649                             |
| Initial v v      | v v — —           | 160         | 160         | 270         | 0.001649                             |

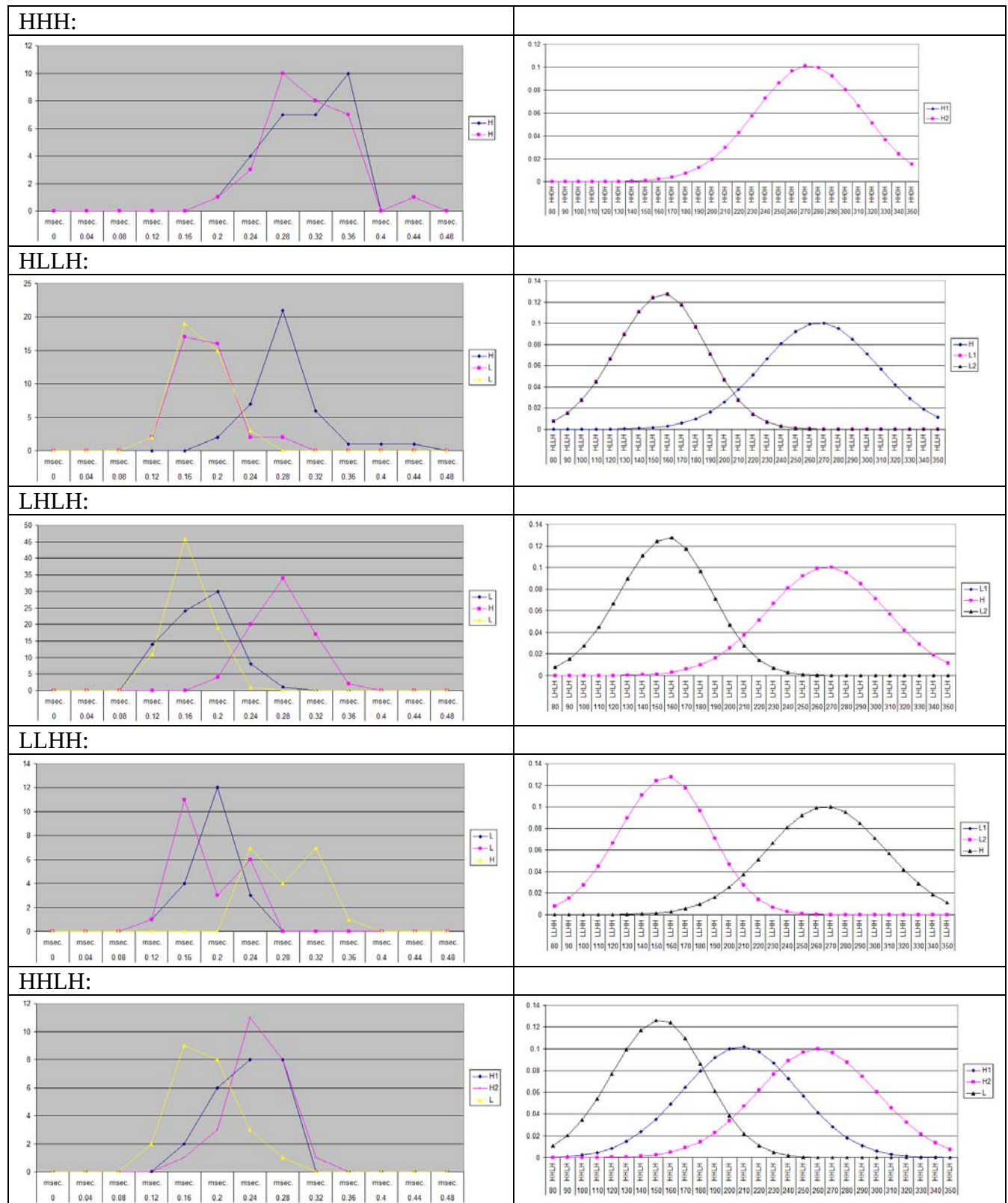
## 30. Comparison with empirical data

|                                       | <i>Shortest</i> | <i>True average</i> | <i>Model Prediction</i> |
|---------------------------------------|-----------------|---------------------|-------------------------|
| ↑                                     |                 |                     |                         |
| Lights in heptamoraic feet            |                 | 154                 | 150                     |
| Lights in hexamoraic feet             |                 | 156                 | 160                     |
| Heavy 1 of heptamoraic foot           |                 | 210                 | 210                     |
| Heavy 2 of heptamoraic foot           |                 | 239                 | 260                     |
| Heavy in a hexamoraic foot with two L |                 | 263                 | 270                     |
| Heavy in a hexamoraic foot with no L  |                 | 286                 | 270                     |
| ↓                                     |                 |                     |                         |
| <i>Longest</i>                        |                 |                     |                         |

## 31. The model creates probability distributions

- We can do a “cross section” of candidates, summing all those with a particular value for a particular syllable.
- This creates histograms that can be compared with the empirical ones given earlier.

### 32. Histograms Comparison: Real on left, theory on right



**33. Is this ready for prime time?**

- I think not, though I'm encouraged by the qualitative behavior.
- I think the next thing to work on is to improve the estimated targets of the constraints — I haven't tried smoothed modes; but intuitively, this ought to be the right target.